

Advances in Industrial Control

Ioan Doré Landau  
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# Adaptive and Robust Active Vibration Control

Methodology and Tests

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 Springer

# **Advances in Industrial Control**

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# Adaptive and Robust Active Vibration Control

Methodology and Tests

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*Ce qui est simple est toujours faux  
Ce qui ne l'est pas est inutilisable*

Paul Valéry  
Mauvaises Pensées

# Series Editors' Foreword

The series *Advances in Industrial Control* aims to report and encourage technology transfer in control engineering. The rapid development of control technology has an impact on all areas of the control discipline. New theory, new controllers, actuators, sensors, new industrial processes, computer methods, new applications, new design philosophies..., new challenges. Much of this development work resides in industrial reports, feasibility study papers and the reports of advanced collaborative projects. The series offers an opportunity for researchers to present an extended exposition of such new work in all aspects of industrial control for wider and rapid dissemination.

It is easy to find examples in everyday life where one experiences the effects of vibration and noise. In fact, there are so many applications where vibration control and/or noise suppression is required that it is difficult to make some form of classification. Virtually every application, domestic and industrial, involving a motor, engine or turbine, for its drive system will have a problem with vibration and/or noise and will invariably require mechanisms or techniques to suppress them. Over a number of years this diversity of applications has been investigated from a control system's point of view by Prof. Ioan Landau and his team of researchers and engineering consultants. The comprehensive results of this study and research are presented in this *Advances in Industrial Control* monograph *Adaptive and Robust Active Vibration Control: Methodology and Tests* by Ioan Doré Landau, Tudor-Bogdan Airimitoiaie, Abraham Castellanos-Silva and Aurelian Constantinescu.

The advantage of a systems-engineering approach to any diverse set of similar industrial problems, in a wide range of applications, is the emergence of a generic study framework that rises above the specific applications. This also allows the application of solution methods from the now well-developed and extensive toolbox of control design methods. At a later stage, such generic solutions can then be tailored for particular application studies.

Professor Landau and his team followed this approach with a focus on active vibration control and active noise control, identifying and classifying along the way

the type of system disturbances for which rejection is required. In many ways the focus on the signal structure of the disturbance represents a way of classifying each type of application. This in-depth understanding of the disturbances enables Prof. Landau and his team to construct solutions from the robustness and adaptive control design paradigms.

An important contribution reported in the monograph is the three physical benchmark laboratory units at the GIPSA-LAB Grenoble. These benchmark installations are described in the monograph and are used to test different aspects of vibration control. The monograph also archives the models and data so that other researchers in the field may use them for further study.

What can the reader expect from this excellent monograph? Professor Ioan Doré Landau is an eminent control engineer who has had a long and fruitful career in the control community, notably acting as the Research Director at the National Centre for Scientific Research at Grenoble. His books, monographs and papers are known for their clarity, and scholarship. He and his team of researchers have produced a monograph that continues this trademark characteristic in the presentation of control concepts and results. The monograph is complete with laboratory experimental results and the theory is supported by instructive appendices. It is an exemplar for the *Advances in Industrial Control* monograph series.

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# Preface

Attenuation of vibration and noise constitutes a growing concern in today's human activities. For more than 45 years, it was realized that passive attenuation of vibration and noise via dedicated absorbers has limits and the concepts of active vibration and noise control have emerged. Active vibration and noise control are strongly related to control methodology even if in the past the control community was not the driving force in this field. Almost from the beginning, the uncertainties and changes in the characteristics of the environment (vibrations, noise, system dynamics) have prompted the idea of using an adaptive approach in active vibration or noise control. Addressing some of these issues from a robustness point of view is a much more recent tendency in the field. Practical experience has shown also the limitations of using only physical models for designing active vibration or noise control systems bringing to light the need of dynamic model identification directly from input/output data.

The aim of this book is to approach the design of active vibration control systems from the perspective of today's control methodology. In that sense the first objective is to formulate from the beginning the various design problems encountered in active vibration control as control problems and search for the most appropriate control tools to solve them. Experimental validation of the proposed solutions on relevant test benches is another issue addressed in this book. To make these techniques widely accepted, an appropriate presentation should be given, eliminating theoretical developments unnecessary for the users (which can be found elsewhere) and focusing on algorithms' presentation and their use. Nevertheless, the proposed solutions cannot be fully understood and creatively exploited without a clear understanding of the basic concepts and methods and so these are given in-depth coverage. The book is mainly based on the work done in a number of Ph.D. theses prepared at Gipsa-lab (INPG/UJF/CNRS), Grenoble, France:

- A. Constantinescu "Robust and adaptive control of an active suspension" [1];
- M. Alma "Adaptive rejection of disturbances in active vibration control" [2];

- T.B. Airimitoiaie “Robust control and tuning of active vibration control systems” [3]; and
- A. Castellanos-Silva “Feedback adaptive compensation for active vibration control in the presence of plant parameter uncertainties” [4];

as well as on the results of an international experimental benchmark on adaptive feedback vibration attenuation [5].<sup>1</sup>

All the methods and algorithms proposed in the book have been thoroughly validated experimentally on three test benches (designed by Mathieu Noé from Paulstra—Vibrachoc, Paris) and located at the Gipsa-lab (INPG/UJF/CNRS) in Grenoble, France.

The idea of writing this book arose when I was asked to present a tutorial on control tools for active vibration control at the 4ème Colloque francophone “Analyse Vibratoire Expérimentale”, Blois, France, November 2014 (Chairman: Roger Serra, INSA Centre Val de Loire). On that occasion, I listed the concepts, methods and algorithms that have been used to provide solutions for active damping, feedback and feedforward attenuation of vibration. All these concepts and methods, which form the basis of the solutions proposed, are taught separately in various control courses or can be found in various books, so it appeared reasonable to try to bring them together and present them accessibly for those interested in using modern control concepts in active vibration control. With this knowledge to hand, the various solutions proposed for active vibration control can be easily understood and used. The need for including experimental results in order to allow readers to assess the potential of the various solutions is obvious.

Three major problems are addressed in the book:

- Active damping (for improving the performance of passive absorbers);
- Adaptive feedback attenuation of single and multiple tonal vibrations; and
- Feedforward and feedback attenuation of broad-band vibrations.

With few exceptions, the analytical details have been skipped and the reference to the appropriate journal papers has been made. The focus is on enhancing motivations, algorithms presentation and experimental evaluations.

Once I had a clear view of how this book should be, I solicited the collaboration of Tudor-Bogdan Airimitoiaie, Abraham Castellanos-Silva and Aurelian Constantinescu in order to realize it.

## Website

Complementary information and material for teaching (simulators, algorithms and data files) can be found on the book website: <http://www.landau-adaptivecontrol.org/>

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<sup>1</sup>[http://www.gipsa-lab.grenoble-inp.fr/~ioandore.landau/benchmark\\_adaptive\\_regulation](http://www.gipsa-lab.grenoble-inp.fr/~ioandore.landau/benchmark_adaptive_regulation)

## Expected Audience

The book may be considered as the basis of a course for graduate students in mechanical, mechatronic, industrial electronic, aerospace and naval engineering.

Part of the book may be used to illustrate the applicability of various graduate control courses (system identification, adaptive control, robust control).

The book is of interest for practising engineers in the field of active vibration control wishing to acquire new concepts and techniques well validated in practice.

The book is also of interest for the people concerned with active noise control, since the techniques presented can, to a large extent, be used for active noise control too. Researchers in the field of active vibration control may also find inspiring material that opens paths toward new developments.

## About the Content

The book is divided into six parts. The introductory part (Chaps. 1 and 2) presents the problems addressed in the book and the test benches used for experimental validation.

The second part is dedicated to the presentation of the control techniques used effectively in active vibration control. Chapter 3 discusses the discrete-time model representation used throughout the book. Chapter 4 is dedicated to the presentation of the parameter adaptation algorithms that will be used throughout the book. Chapter 5 gives a compact presentation of system identification techniques focusing on the specific algorithms used in active vibration control. Chapter 6 illustrates the use of these identification techniques for identifying the dynamic models of the three test benches already presented in Chap. 2. Chapter 7 reviews basic methods for the design of digital controllers that have been used in active vibration control. Chapter 8 provides effective solutions for identification in closed-loop operation allowing the improvement of the dynamic models identified in open-loop operation or re-tuning of the controller. Chapter 9 addresses the problem of controller order reduction because the result of the design is often a high-order controller; since on the one hand the models of the system are of high dimension and on the other the robustness constraints contribute to the increase of the order of the controller.

The third part is dedicated to the problem of active damping (Chap. 10). The design aspects and the experimental evaluation are discussed in detail.

The fourth part is concerned with the robust and adaptive attenuation of vibrations by feedback. Chapter 11 treats the problem of robust feedback attenuation of narrow-band (tonal) disturbances subject to limited frequency variations. Chapter 12 introduces the basic algorithm for adaptive attenuation of narrow-band disturbances. Experimental evaluations on two test benches are presented. Performance comparison of robust and adaptive solutions is provided. Chapter 13 is specifically dedicated to the problem of attenuating multiple unknown and time-varying

vibrations. Two algorithms specifically developed for this problem will be presented and their performance and complexity will be compared with those of the basic algorithm presented in Chap. 12.

In the fifth part of the book we consider feedforward compensation of disturbances, which has to be used when the bandwidth of disturbances (vibrations) is such that the performance/robustness compromise cannot be conveniently satisfied by feedback alone. Chapter 14 examines the linear design, which has to be done from data (since the model of the disturbance is unknown and it should be identified from data). Chapter 15 provides adaptive solutions for infinite impulse response (IIR) feedforward compensation as well as experimental results illustrating the performance of such systems in various situations. Chapter 16 provides adaptive solutions for Youla–Kučera feedforward compensator configuration. Experimental comparison between the two configurations concludes the chapter.

Part six of the book contains five appendices. Appendix A is dedicated to the *generalized stability margin* and the *Vinnicombe distance* between two transfer functions: two very useful concepts in system identification in closed-loop operation and controller reduction. Appendix B details the numerically safe implementation of parameter adaptation algorithms in real time. Appendix C details the derivation of an adaptation algorithm used in Chap. 13 for rejection of narrow-band disturbances. Appendix D details the derivation of explicit equations for the residual force or acceleration in the context of adaptive feedforward compensation. These equations allow the straightforward definition of the appropriate parameter adaptation algorithm. Finally, Appendix E gives the details and experimental evaluation of an *integral plus proportional* parameter adaptation algorithm (IP-PAA adaptation), which adds a “proportional” component to the classical “integral” parameter adaptation algorithms.

There are 271 references disseminated at the end of each chapter.

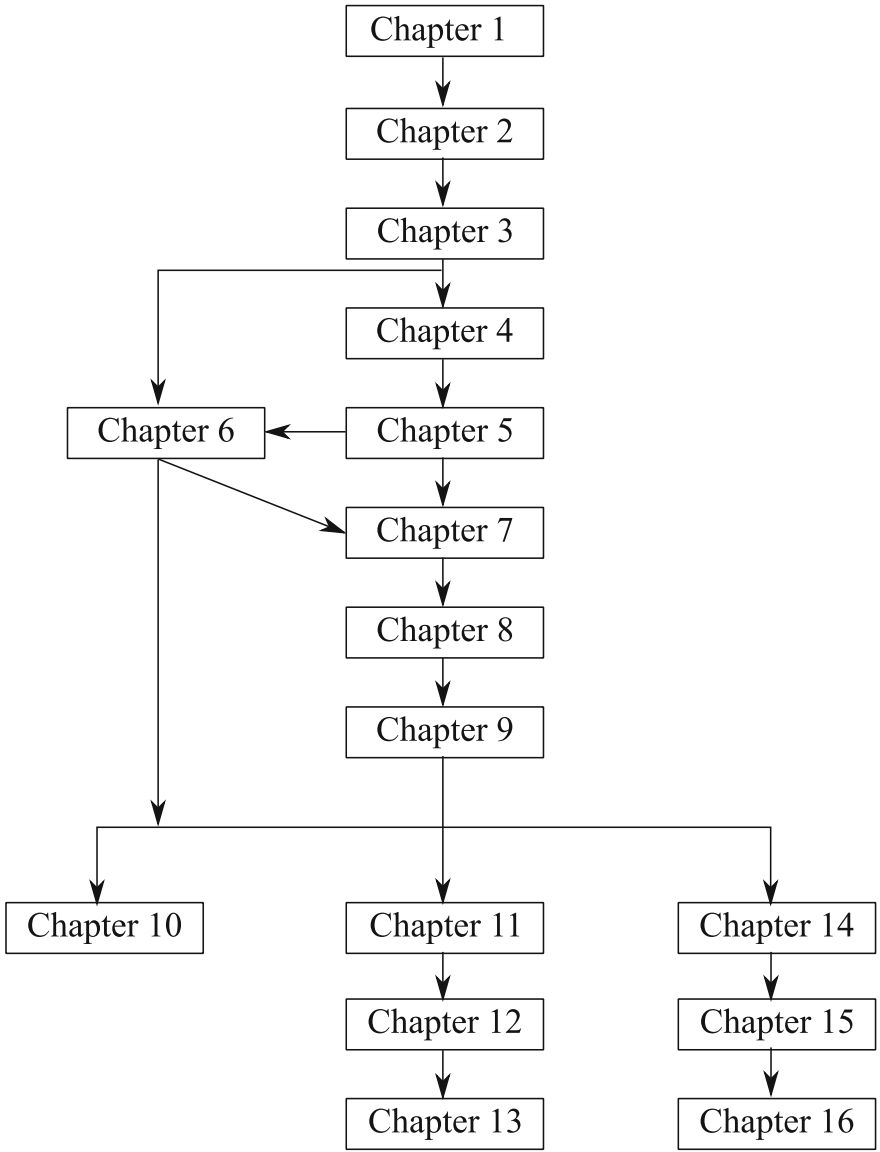
## Pathways Through the Book

For a course on the subject, the Chaps. 1–9 have to be covered first followed, in no particular order, by Parts III, IV or V.

For experts in digital, robust and adaptive control, Chaps. 3, 4, 5, 7, 8, and 9 can be skipped and again Parts III, IV and V can be read in any order.

An image of the applicability of the results can be easily obtained by reading Chap. 2 and the sections concerning experimental results in Chaps. 10–16.

Figure 1 gives a view of the interdependence of the various chapters.



**Fig. 1** Pathways through the book

## Acknowledgements

I would like first to thank M. Noé, who on the one hand designed the bench tests and on the other hand pointed out the pertinent problems to be solved in active vibration control. The long, steady interaction between us was a major driving factor in our research on active vibration control.

I would like to thank M. Alma, whose contributions to the field of active vibration control are reflected in the book.

I would like to thank D. Rey, G. Buche and A. Franco for their involvement in the research project and the technical support in operating the test benches.

Over the years, working in the area of active vibration control, I have had the privilege of interacting with a number of colleagues among whom I would like to mention: B.D.O. Anderson, S. Aranovski, F. Ben Amara, R.B. Bitmead, D. Bonvin, M. Bodson, R.A. de Callafon, X. Chen, L. Dugard, T. Hélie, P. Ioannou, C.R. Johnson, A. Karimi, J. Langer, F.L. Lewis, J.J. Martinez, G. Ruget, R. Serra, M. Tomizuka, S. Valentinotti, Z. Wu. I would like to express my appreciation for their contributions.

The long-term support of the Centre National de la Recherche Scientifique (CNRS) and of the GIPSA-LAB Grenoble (Institut National Polytechnique de Grenoble, Université Joseph Fourier, CNRS) is gratefully acknowledged.

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Grenoble, France  
April 2016

Ioan Doré Landau

## References

- [1] Constantinescu, A.: Commande robuste et adaptative d'une suspension active. Thèse de doctorat, Institut National Polytechnique de Grenoble (2001)
- [2] Alma, M.: Rejet adaptatif de perturbations en contrôle actif de vibrations. Ph.D. thesis, Université de Grenoble (2011)
- [3] Airimitoiaie, T.B.: Robust design and tuning of active vibration control systems. Ph.D. thesis, University of Grenoble, France, and University "Politehnica" of Bucharest, Romania (2012)
- [4] Castellanos-Silva, A.: Compensation adaptative par feedback pour le contrôle actif de vibrations en présence d'incertitudes sur les paramètres du procédé. Ph.D. thesis, Université de Grenoble (2014)
- [5] Landau, I.D., Silva, A.C., Airimitoiaie, T.B., Buche, G., Noé, M.: Benchmark on adaptive regulation—rejection of unknown/time-varying multiple narrow band disturbances. *European Journal of Control* **19**(4), 237—252 (2013). <http://dx.doi.org/10.1016/j.ejcon.2013.05.007#1>

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